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## The Orbital Diameter of Primitive Permutation Groups

Let  $G$  be a group acting transitively on a finite set  $\Omega$ . Then  $G$  acts on  $\Omega \times \Omega$  componentwise. Define the orbitals to be the orbits of  $G$  on  $\Omega \times \Omega$ . The diagonal orbital is the orbital of the form  $\Delta = \{(\alpha, \alpha) | \alpha \in \Omega\}$ . The others are called non-diagonal orbitals. Let  $\Gamma$  be a non-diagonal orbital. Define an orbital graph to be the non-directed graph with vertex set  $\Omega$  and edge set  $(\alpha, \beta) \in \Gamma$  with  $\alpha, \beta \in \Omega$ . If the action of  $G$  on  $\Omega$  is primitive, then all non-diagonal orbital graphs are connected. The orbital diameter of a primitive permutation group is the supremum of the diameters of its non-diagonal orbital graphs.

There has been a lot of interest in finding bounds on the orbital diameter of primitive permutation groups. In my talk I will outline some important background information and the progress made towards finding specific bounds on the orbital diameter. In particular, I will discuss some results on the orbital diameter of the groups of simple diagonal type and their connection to the covering number of finite simple groups. I will also discuss some results for affine groups, which provides a nice connection to the representation theory of quasisimple groups.

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