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## ***k*-closures of finite nilpotent permutation groups**

Let  $G$  be a permutation group on a finite set  $\Omega$ . Denote the set of orbits of the componentwise action of  $G$  on  $\Omega^k$  by  $\text{Orb}(G, \Omega^k)$ . Wielandt [1] defined the  $k$ -closure of  $G$  to be the group

$$G^{(k)} = \text{Aut}(\text{Orb}(G, \Omega^k)) = \{g \in \text{Sym}(\Omega) \mid O^g = O \forall O \in \text{Orb}(G, \Omega^k)\}.$$

A permutation group is called  $k$ -closed if  $G = G^{(k)}$ . In this talk we discuss  $k$ -closures of nilpotent groups.

**Theorem.** If  $G$  is a finite nilpotent permutation group, and  $k \geq 2$ , then  $G^{(k)}$  is the direct product of  $k$ -closures of Sylow subgroups of  $G$ .

This theorem generalizes results of [2,3] and provides a criterion of the  $k$ -closedness for finite nilpotent permutation groups.

**Corollary.** For  $k \geq 2$ , a finite nilpotent permutation group  $G$  is  $k$ -closed if and only if every Sylow subgroup of  $G$  is  $k$ -closed.

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### **References**

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